

N+1 CHALLENGES FOR SLE

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outline

- give up trees
- tend to your meta-language
- the metalevel is not the world of static
- diversify
- escape the empiricism trap
- ...
- +1

GIVE UP TREES

or: embrace the modelling community

give up trees

- not everything is a tree
- just like not everything is a function
- for everything is in fact a relation
- just like everything is a graph

- in modelling, a tree is just a degenerate graph
 - undercut only by lists

give up trees

trees vs. graphs
PL vs. SE (Albert Zündorf)
mathematical rigour vs. empiricism
hard science vs. soft science

give up trees

- but trees are great
- inductive definitions
- inductive proofs

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Inductive graphs and functional graph algorithms

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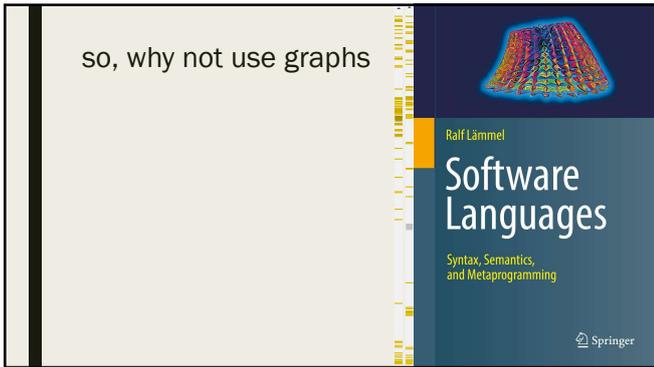
Abstract

We propose a new style of writing graph algorithms in functional languages which is based on an inductive view of graphs as mathematical abstract data types. We show how the graph model can be implemented efficiently, and how to implement low graph algorithms using OCaml's pattern-matching facilities. We also discuss how to extend the graph model to include directed graphs. We also regard this as a contribution to the teaching of algorithms and data structures in functional languages, since we can use the inductive-style graph algorithms instead of the imperative algorithms that are standard today.

1 Introduction

How do we implement a graph algorithm in a functional programming language? This seemingly simple question has several answers. For quite a long time, and there are many different proposals to how to do so. Of course, it is not really difficult to describe graph algorithms in functional languages. The real challenge is to obtain clear and elegant programs, that is, functional programs that do not lose their elegance and simplicity and that have the same asymptotic complexity as imperative ones.

The main difficulty that arises when dealing, for example, with graph traversal



conjecture:

the linear nature of our language(s) makes us prefer trees over graphs

text bla bla $a(b, c)$ bla bla text

text bla bla $((a, b), (a, c))$ bla bla text

needs building up a mental environment (dictionary)

$$\begin{array}{c} a \\ \swarrow \quad \searrow \\ b \quad c \end{array}$$

$a(b, a)$

$$\begin{array}{c} a \\ \swarrow \quad \searrow \\ b \quad c \end{array}$$

$\{(a, b), (a, a)\}$

$$\begin{array}{c} a \\ \swarrow \quad \searrow \\ b \quad a \end{array}$$

$a(b, "a")$

The Graph Paradox:
In working with graphs, we resort to trees.

(i.e., we express the general in terms of the special, while it should be the other way round)

caused by language

- ### give up trees
- trees go with functions
 - like graphs go with relations
 - has SLE a preference for functional metalanguages?
 - adoption of functional PL constructs in language definitions and proofs
 - *Maybe and Either monads in Isabelle*
 - *List monads, too?*
 - *not needed in relational languages?*
 - *are functions a source of accidental complexity?*
 - if the linearity of metalanguages suggests trees, is progress slowed by the linearity of metalanguages?

TEND TO YOUR META-LANGUAGE

tend to your metalanguage

28 Varieties of Substitution Notation: POPL 1973–2016

$e[x]$	1	$e[v/x]$	133	$e(v/x)$	1
$e[x]$	1	$e[v/x]$	6	$e\{v/x\}$	25
$[v/x]e$	67	$e[v/x]$	2	$e\{v/x\}$	5
$\{v/x\}e$	1	$e[v/x]$	1	$e\{v/x\}$	4
$[x := v]e$	2	$e[v/x]$	5	$e\{x \leftarrow v\}$	4
$\{x := v\}e$	9	$e[x \leftarrow v]$	21	$e\{x \rightarrow v\}$	1
$[v/x]e$	1	$e[x \leftarrow v]$	7	$e\{x \rightarrow v\}$	1
$\{v/x\}e$	2	$e[x \rightarrow v]$	17	$e\{\{v/x\}\}$	2
$\{x \rightarrow v\}e$	6	$e[x \rightarrow v]$	2	$e\{\{x \leftarrow v\}\}$	1
	4				

* Used by H. P. Barendregt in *The Lambda Calculus: Its Syntax and Semantics* (1980).
Most popular during 1973–2016 are highlighted. Usage has grown over time; substitution used in over 1/3 of POPL papers 2012–2016.

Guy Steele:
"It's Time for a
New Old Language"
(2017 ACM PPoPP Keynote)

ORACLE

tend to your metalanguage

- what are these?
 - "unenclosed sequence", "unpacked collection"
- that we can still read this texts mean high redundancy
 - can squeeze even more on a page
- common metalanguage?
 - LaTeX!
 - but that's a meta-metalanguage
- how about a standard metalanguage?

$$e^* \quad e_1 \dots e_n \quad \bar{e}$$

USLES

tend to your metalanguage

- how about choosing one with precise syntax and semantics?
- how about an executable one?
- theorems and proofs about properties of the object language ...
- ... become program verification (verification of the interpreter)
 - [P] S [R]
- how about a programming language as metalanguage?
 - Haskell?
 - Coq?

how about PROLOG?

$$\frac{(S, e_1) \Rightarrow (S', v_1) \quad (S', e_2) \Rightarrow (S', v_2)}{v = v_1 + v_2} \frac{(S, e_1 + e_2) \Rightarrow (S', v)}$$

$$\frac{(S, e) \Rightarrow (S', v) \quad \text{def}(f(x)) = e'}{(S', \left[\frac{x}{v} \right] e') \Rightarrow (S', v')} \frac{(S, f(e)) \Rightarrow (S', v')}$$

(S, E1 + E2) => (S1, V) :-
 (S, E1) => (S2, V1),
 (S2, E2) => (S1, V2),
 V is V1 + V2.

(S, f(F, E)) => (S1, V1) :-
 (S, E) => (S2, V),
 def(F, V, E1),
 (S2, E1) => (S1, V1).

:- ([x=1, y=2], x+y) => (S, V).
 yes: S = [x=1, y=2], V = 3

:- ([z=3], fak(z)) => (S, V).
 yes: S = [z=3], V = 6

:- ([x=1, y=2], x*y) => (S, V).
 no

:- ([z=-1], fak(z)) => (S, V).
 ..

:- ([x=1], x+y) => (S, V).
 no

is PROLOG relational?

?- f(X) = Y, g(Y) = X.

with occurs-check turned on?

THE METALEVEL IS NOT THE WORLD OF STATIC

or: make editing a discipline

the metalevel is not the world of static

- static semantics (strong typing) are standard on the metalevel
- what about dynamic semantics?
- dynamic semantics for
 - transformation (*sure, the compiler*)
 - editing
 - synthesis
 - (*incl. refactoring*)
- with various soundness guarantees for the object level
 - change a program, guarantee that it still compiles
 - change a language and its programs with it, with strong guarantees

DIVERSIFY

or: software language tools are not the only programs of interest

SLE
=
the metacircular science of metacircularity

we live on our own dog food

diversify

conjecture:

For a substantial number of students,
a compiler is the only program they have ever written
or even seen.

They view everything as a function/tree.

diversify

- ok for research in SLE
- sufficient for having impact?
- 80% of software is embedded
 - security and realtime as important as safety
 - persistence, distribution, and roll-back
- compared with medicine (engineering), SLE has no impact over what is happening in the wild
 - medical societies control everything related to diagnosis and treatment
 - we control nothing
 - even though humankind is subjected to programmers' doing

diversify

conjecture:

To get impact, we need to embrace all software.

ESCAPE THE EMPIRICISM TRAP

or: let's formalize utility

escape the empiricism trap

- from SE, student experiments, questionnaires
- instead find and establish good analytical models of judging the utility of SLE tools
- not number of keystrokes, but perhaps number of decisions to be made
- (game theory)
- validate the model once, then work with it forevermore
- (like the mouse model in pharmaceuticals)
- good models are hard to find (corona)
- field of study is language
- not a specific language, not even all existing languages, but all languages that can be conceived of
- infinite study space
- make the best of this freedom
- stop doing things in a way that "because the proofs are easier" that's a road to insignificance

escape the empiricism trap

- medicine is evidence-based
 - *doctors want proofs*
- our formally proving is great
- but restricts progress to the formally provable
- drives progress to the formally provable
 - *I know how to prove it, so I propose it*
- how do I prove that x is good or bad?

escape the empiricism trap

- empirical experiments
 - *hard to do*
- all our empirical experiments are psychological experiments
- confounding factors hard to control
- its mathematics are unknown (for many of us)
- generalization is hard to show

escape the empiricism trap

- medical (pharmaceutical) research works with models
 - *mouse model*
- each new treatment requires a new study on humans
- each new treatment requires a new study on mice
- one study showing that studies on mice allow predictions for humans
- we can't get mice to code

escape the empiricism trap

- programming with tools is a game
 - with *players* programmer and tools
 - each *taking turns*
 - tools provide clues
 - programmer decides
- programming = working off one giant decision graph (or tree?)
- find mathematical models
- show how tools reduce the size of the graph
- one final experiment showing that model is valid

HOW TO TYPE THAT DAMN PARENT ATTRIBUTE?

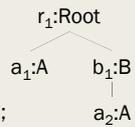
or: if you can't type this, what can you do?

how to type that damn parent attribute?

```
node type Root begin a : A; b : B end;
```

```
node type A begin parent() : Root end;
```

```
node type B begin a : A; parent() : Root end;
```



```
a1.parent().parent()    static error
a2.parent().parent()    static error
```